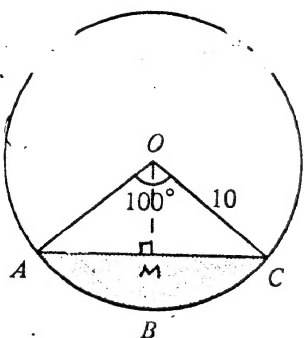
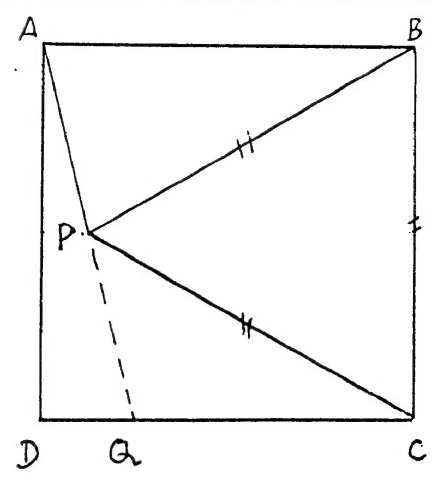
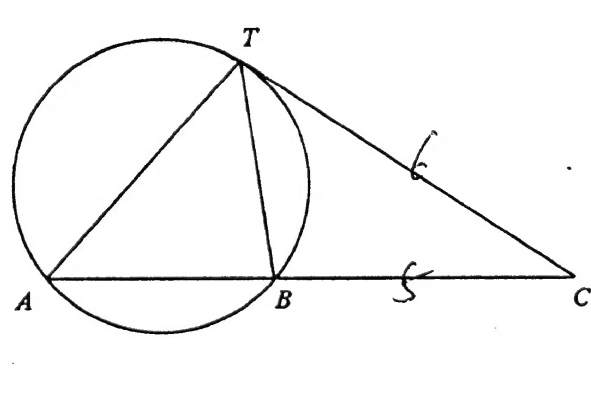


Solutions	Marks	Remarks
<p>5. (a) Area of $OABC = \pi 10^2 \times \frac{100^\circ}{360^\circ}$ $= 87.27$ (corr. to 2 d.p.) (or 87.28)</p> <p>(b) Area of $\triangle OAC = \frac{1}{2} \times 10 \times 10 \times \sin 100^\circ$ $= 49.24$ (corr. to 2 d.p.)</p> <p>(c) Area of minor segment ABC $= 87.27 - 49.24$ $= 38.03$ (corr. to 2 d.p.) (or 38.04)</p>	<p>1M</p> <p>1A</p> <p>1M</p> <p>1A</p> <p>1M</p> <p>1A</p> <p>1A</p> <p>6</p>	<p>$\Delta = \frac{1}{2} AC \times OM$ $= \frac{1}{2} \times 15.3209 \times 6.4279$ $= 49.24$... 1M ... 1A</p> 
<p>6. $\log 2 = r$, $\log 3 = s$.</p> <p>(a) $\log 18 = \log 2 \times 3^2$ $= \log 2 + \log 3^2$ $= \log 2 + 2 \log 3$ $= r + 2s$</p> <p>(b) $\log 15 = \log 3 \times 5$ $= \log 3 + \log 5$ $= \log 3 + \log \frac{10}{2}$ $= \log 3 + \log 10 - \log 2$ $= 1 - r + s$</p>	<p>1A</p> <p>1M</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>1A</p> <p>6</p>	<p>For $18 = 2 \times 3^2$ $\log ab = \log a + \log b$ or $\log a^2 = 2 \log a$</p> <p>For $5 = \frac{10}{2}$ or $15 = \frac{30}{2}$</p>
<p>7. (a) The coordinates of the centre are given by $x = -(-\frac{4}{2})$, $y = -\frac{10}{2}$ i.e. $x = 2$, $y = -5$</p> <p>(b) As C touches the y-axis, its radius = 2 $4 + 25 - k = 2^2$ $k = 25$</p>	<p>1M</p> <p>1A</p> <p>1M+1A</p> <p>1M</p> <p>1A</p> <p>6</p>	<p>Centre = 2, -5 (Pf-1)</p> <p>OR</p> <p>Subs. $(0, -5)$ 1M $25 - 50 + k = 0$ $k = 25$ 1A $r = \sqrt{4 + 25 - 25}$ 1M $= 2$ 1A</p> <p>OR</p> <p>Put $x = 0$, $y^2 + 10y + k = 0$ has equal roots. 1M $100 - 4k = 0$ $k = 25$ 1A $r = \text{etc.}$</p>

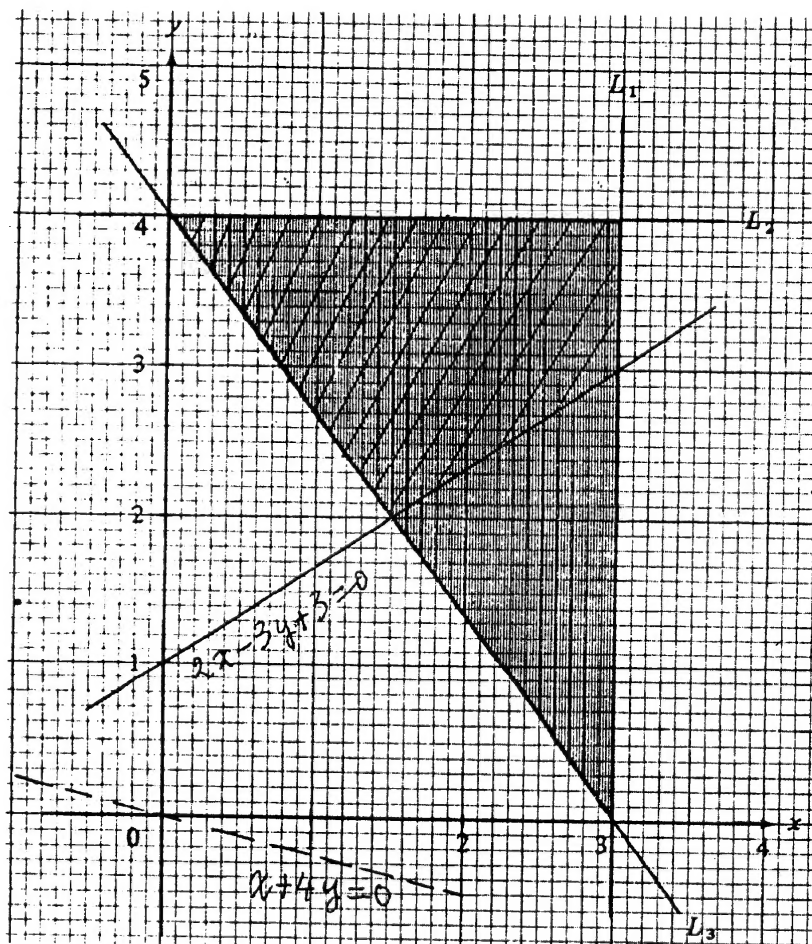
Solutions	Marks	Remarks
<p>8. (a) (i)</p> 		<p>ABCD in order</p> <p>1 For P</p> <p>1 For Q (between D, C)</p>
<p>(ii) Since $\triangle PBC$ is equilateral, $\angle PBC = 60^\circ$</p> <p>$\angle ABP = 90^\circ - 60^\circ = 30^\circ$</p> <p>As $BA = BP$, $\angle PAB = \frac{1}{2}(180^\circ - 30^\circ)$</p> <p>$= 75^\circ$</p> <p>Since $AB \parallel DC$, $\angle PQC = 180^\circ - 75^\circ$</p> <p>$= 105^\circ$</p>	<p>1A</p> <p>1M</p> <p>1A</p> <p>1M</p> <p>1A</p>	<p>Follow through even if diagram not accurate</p> <p>or equivalent</p> <p>OR</p> <p>$\angle PAD = 15^\circ$</p> <p>$\angle PQC = 90^\circ + 15^\circ = 105^\circ$</p>
<p>(b) (i) $\triangle TCB$ is similar to $\triangle ACT$ because</p> <p>$\angle C$ is common.</p> <p>$\angle BTC = \angle BAT$ (angle in alternate segment)</p> <p>(ii) $\frac{AC}{CT} = \frac{CT}{BC}$</p> <p>$AC = \frac{6^2}{5} = 7.2$</p> <p>$\therefore AB = 7.2 - 5$</p> <p>$= 2.2 \left(= \frac{11}{5} \right)$</p>	<p>1</p> <p>1</p> <p>1A</p> <p>1A</p> <p>1A</p>	<p>$\angle BTC$ 寫成 $\angle T$</p> <p>(pp-1)</p> <p>Indication of 2 pairs of equal angles. With held if proving congruence.</p> <p>Follow through even if (b)(i) wrong.</p>
		

Solutions

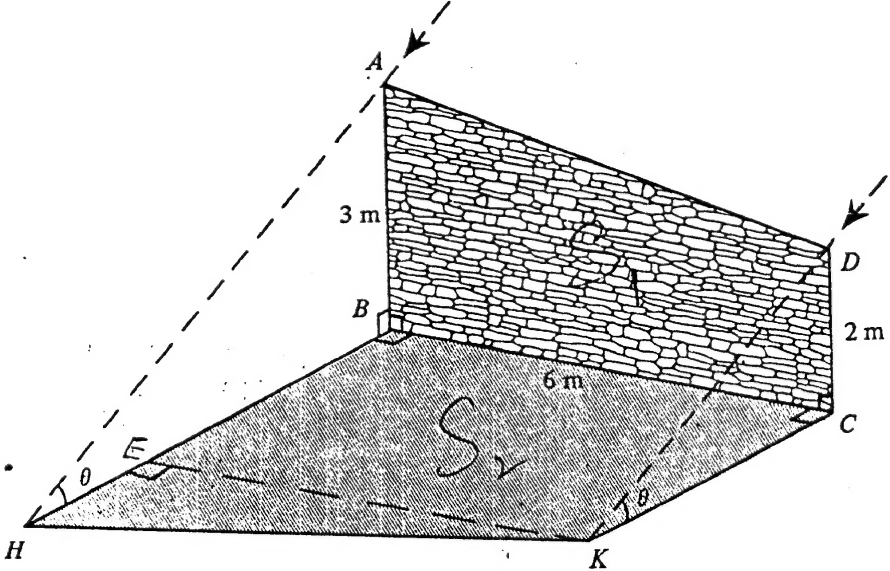
Solutions	Marks	Remarks
<p>9. (a) Between 100 and 999, the smallest multiple of 7 is 105, the largest is 994.</p>	<p>1A <u>1A</u> 2</p>	
<p>(b) The number of multiples is $\frac{994 - 105}{7} + 1$ = 128</p>	<p>2M 1A</p>	<p>OR $994 = 105 + (n-1) \times 7$</p>
<p>The sum of these multiples = 105 + 112 + ... + 994 = $\frac{128}{2} [105 + 994]$ = 70336</p>	<p>2M <u>1A</u> 6</p>	<p>$\frac{994}{7} - \frac{105}{7} + 1$ = $142 - 15 + 1$ = 128</p>
<p>(c) The sum of all positive 3-digit integers = 100 + 101 + ... + 999 = $\frac{900}{2} [100 + 999]$ = 494,550</p>	<p>1 1A</p>	
<p>The required sum = 494,550 - 70,336 = 424,214</p>	<p>1M <u>1A</u> 4</p>	

Solutions	Marks	Remarks
<p>10. (a) Let $y = k_1x + k_2x^2$, where k_1 and k_2 are constants.</p> <p>Putting $x = 1, y = -5; x = 2, y = -8$, we have</p> $k_1 + k_2 = -5 \dots\dots\dots$ $2k_1 + 4k_2 = -8$ <p>Solving, $k_1 = -6, k_2 = 1$</p> $\therefore y = -6x + x^2$ <p>Putting $x = 6$, we have $y = 0$.</p> <p>(b) $y = -6x + x^2 = (x^2 - 6x + 9) - 9$</p> $= (x - 3)^2 - 9 \dots\dots\dots$ <p>When $x = 3$, the value of y is least and the least value is -9.</p>	<p>2</p> <p>1M</p> <p>1A</p> <p>1A</p> <p>1A+1A</p> <p>1A</p> <p>8</p> <p>1M</p> <p>1A</p> <p>1M+1A</p> <p>4</p>	<p>For $y=kx+kx^2$ or $y = kx+x^2$</p> <p>or $y = x+kx^2 \dots\dots\dots 1$</p> <p>$y = x + x^2$</p> <p>$y = k_1x$</p> <p>$y = k_2x^2$ } no mark.</p> <p>Equality must hold.</p>
<p>11. (a) From the curve,</p> <p>(i) the median is 70 marks.</p> <p>(ii) the 1st quartile is 50 marks.)</p> <p>the 3rd quartile is 86 marks.) $\dots\dots$</p> <p>\therefore the interquartile range = $86 - 50$</p> <p>= 36 marks</p> <p>(b) (i) From the curve, the number of prize-winners = 60.</p> <p>(ii) The probability that the student is a prize-winner = $\frac{60}{600} (= \frac{1}{10})$.</p> <p>(iii)(1) The probability that both are prize-winners is $\frac{60}{600} \times \frac{59}{599} = \frac{59}{5990} (=0.01)$</p> <p>(2) The probability that both are not prize-winners = $\frac{540}{600} \times \frac{539}{599} (= \frac{4851}{5990}) (=0.81)$</p> <p>$\therefore$ the probability that at least one is a prize-winner = $1 - \frac{4851}{5990}$</p> <p>$\frac{60}{600} \cdot \frac{540}{599} + \frac{540}{600} \cdot \frac{60}{599} + \frac{60}{600} \cdot \frac{60}{599} = \frac{1139}{5990} (=0.19)$</p>	<p>1A</p> <p>1A</p> <p>1M</p> <p>1A</p> <p>4</p> <p>1A</p> <p>1M+1A</p> <p>1M+1A</p> <p>1A</p> <p>1M</p> <p>1A</p> <p>8</p>	<p>for either</p> <p>$(86 \pm 3) - (50 \pm 3)$</p> <p>Accept $\frac{1}{10} \times \frac{1}{10} = \frac{1}{100}$</p> <p>1M for product rule</p> <p>Accept $\frac{9}{10} \times \frac{9}{10}$</p> <p>OR</p> <p>$\frac{9}{10} \times \frac{60}{599} + \frac{1}{10} \times \frac{540}{599}$</p> <p>$+ \frac{1}{10} \times \frac{59}{599}$ 1M+1A</p> <p>$= \frac{1139}{5990} \dots\dots\dots 1A$</p>

Solutions	Marks	Remarks
12. (a) L_3 is given by $\frac{x}{3} + \frac{y}{4} = 1$ $\frac{y-0}{4-0} = \frac{4-0}{0-3}$ i.e. $4x + 3y = 12$	1M <u>1A</u> 2	or 2-pt form, etc. Must be in this form.
(b) The three constraints are $y \leq 4$ $x \leq 3$ $4x + 3y \geq 12$	1A 1A <u>1A</u> 3	Withhold 1 mark if '=' omitted. or $4x + 3y - 12 \geq 0$.
(c) The line $x + 4y = 6$ drawn in the diagram. From the diagram, P is greatest when $x = 3$, $y = 4$ and least when $x = 3$, $y = 0$. The greatest value of $P = 19$, the least value = 3.	1M+1A 1A 1A 4	For 1A Drop of 2-3 verticle units for 10 horizontal units. OR Testing any vertices 1M At (3, 0), $P = 3$. At (0, 4), $P = 16$. At (3, 4), $P = 19$. 1A



(d) The line $2x - 3y + 3 = 0$ drawn in the diagram. The shaded region. P is least when $x = \frac{3}{2}$, $y = 2$. The least value = $\frac{19}{2}$ (= 9.5)	1A 1A <u>1A</u> 3	± 1 unit at (1.5, 2), (3, 3). Should be reasonably shaded. At (3, 3), $P = 15$. At (1.5, 2), $P = 9.5$.
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Solutions	Marks	Remarks
<p>13. (a) $\frac{AB}{HB} = \tan\theta$.</p> <p>$HB = \frac{3}{\tan\theta} \text{ m} \dots\dots\dots$</p> <p>$\frac{DC}{KC} = \tan\theta, KC = \frac{2}{\tan\theta} \text{ m}$</p>	<p>1M</p> <p>1A</p> <p>1A</p> <p><u>3</u></p>	<p>Wrong/no unit, pp-1.</p> <p>2 + 1</p>
<p>(b) (i) $S_1 = \frac{6}{2} (3 + 2)$</p> <p>$= 15 \text{ m}^2 \dots\dots\dots$</p> <p>(ii) $S_2 = \frac{6}{2} \left(\frac{3}{\tan\theta} + \frac{2}{\tan\theta} \right)$</p> <p>$= \frac{15}{\tan\theta} \text{ m}^2 \dots\dots\dots$</p>	<p>1A</p> <p>1A</p>	<p>$\frac{15}{\frac{15}{\tan\theta}} = \tan\theta$</p> <p>$\therefore \tan\theta = \tan\theta$ } no merit</p>
<p>$\therefore \frac{S_1}{S_2} = \frac{15}{\frac{15}{\tan\theta}} = \tan\theta$</p>	<p>1A</p>	<p>Must show working.</p>
	<p>$\frac{S_1}{S_2} = \frac{15}{\frac{15}{\tan\theta}} = \tan\theta$</p> <p>↑ 缺寫</p> <p>(pp-1)</p>	
<p>(c) Let $KE \perp BH$.</p> <p>$EK = BC = 6 \text{ (m)}$</p> <p>$HE = \frac{3}{\tan\theta} - \frac{2}{\tan\theta} = \left(\frac{3}{\tan 30^\circ} - \frac{2}{\tan 30^\circ} \right) \text{ m} (= \sqrt{3})$</p> <p>$\therefore HK = \sqrt{HE^2 + EK^2}$</p> <p>$= \sqrt{(\sqrt{3})^2 + 6^2}$</p> <p>$= \sqrt{39} \text{ m} \dots\dots\dots$</p>	<p>1M</p> <p>1A</p> <p>1M+1M</p> <p>1M</p> <p><u>1A</u></p> <p><u>6</u></p>	<p>Construction of perpendicular line</p>

Solutions	Marks	Remarks																		
<p>14. (a) (i) $x^3 - \frac{4}{3}x - 6 = 0$ can be written as</p> $x^3 = \frac{4}{3}x + 6.$ <p>Consider the line $y = \frac{4}{3}x + 6$.</p> <p>It cuts the curve $y = x^3$ at $x = r$,</p> <p>where r lies between 2.0 and 2.1.</p>	<p>1M</p> <p>1A+1A</p> <p>1A</p>	<p><i>optional</i></p> <p>1A for equation 1A for line drawn, ±1 vertical division about (0, 6), (3, 10)</p>																		
<p>(ii) Let $f(x) = x^3 - \frac{4}{3}x - 6$</p> <p>$f(2) = -(-0.67)$</p> <p>$f(2.1) = +(0.46)$</p>	<p>1M</p>	<p><i>optional</i></p> <p>Correct change of sign.</p>																		
<table border="1"> <thead> <tr> <th>Interval</th> <th>Mid-value x</th> <th>$f(x)$</th> </tr> </thead> <tbody> <tr> <td>$2.000 < r < 2.100$</td> <td>2.050</td> <td>$-(-0.12)$</td> </tr> <tr> <td>$2.050 < r < 2.100$</td> <td>2.075</td> <td>$+(0.17)$</td> </tr> <tr> <td>$2.050 < r < 2.075$</td> <td>2.063</td> <td>$+(0.02)$</td> </tr> <tr> <td>$2.050 < r < 2.063$</td> <td>2.057</td> <td>$-(-0.04)$</td> </tr> <tr> <td>$2.057 < r < 2.063$</td> <td></td> <td></td> </tr> </tbody> </table>	Interval	Mid-value x	$f(x)$	$2.000 < r < 2.100$	2.050	$-(-0.12)$	$2.050 < r < 2.100$	2.075	$+(0.17)$	$2.050 < r < 2.075$	2.063	$+(0.02)$	$2.050 < r < 2.063$	2.057	$-(-0.04)$	$2.057 < r < 2.063$			<p>1M+1A</p> <p>1M</p>	<p>1M for choosing mid-value, 1A for correct sign.</p> <p>Next correct step.</p>
Interval	Mid-value x	$f(x)$																		
$2.000 < r < 2.100$	2.050	$-(-0.12)$																		
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$2.057 < r < 2.063$																				
<p>$\therefore r = 2.06$ (correct to 2 d.p.)</p> <p>Alt. Solution:</p> <p>$f(2) = -$</p> <p>$f(2.5) = +$)</p>	<p>1A</p> <p><u>9</u></p> <p>1M</p>	<p><i>optional</i></p>																		
<table border="1"> <thead> <tr> <th>Interval</th> <th>Mid-value x</th> <th>$f(x)$</th> </tr> </thead> <tbody> <tr> <td>$2.000 < r < 2.500$</td> <td>2.225</td> <td>+</td> </tr> <tr> <td>$2.000 < r < 2.225$</td> <td>2.113</td> <td>+</td> </tr> <tr> <td>.</td> <td>.</td> <td>.</td> </tr> <tr> <td>.</td> <td>.</td> <td>.</td> </tr> <tr> <td>.</td> <td>.</td> <td>.</td> </tr> </tbody> </table>	Interval	Mid-value x	$f(x)$	$2.000 < r < 2.500$	2.225	+	$2.000 < r < 2.225$	2.113	+	<p>1M+1A</p> <p>1M</p>	
Interval	Mid-value x	$f(x)$																		
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.	.	.																		
.	.	.																		
.	.	.																		
<p>$\therefore r = 2.06$ (correct to 2 d.p.)</p>	<p>1A</p>																			
<p>(b) Put $x = t + 1$</p> <p>The given equation can be written</p> <p>as $3x^3 - 4x - 18 = 0$</p> <p>or $x^3 - \frac{4}{3}x - 6 = 0$</p> <p>By (a), the solution is</p> <p>$t = 2.06 - 1$</p> <p>$= 1.06$ (correct to 2 d.p.)</p>	<p>1A</p> <p>1A</p> <p>1M</p> <p>1A</p> <p><u>3</u></p>																			

Solutions

Marks

Remarks

14.

